The Missing Link: Labor Share and Monetary Policy

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Motivation

- Structural models for Monetary Policy (MP) analysis that rely on nominal rigidities establish clear transmission mechanisms from MP shocks to real economic activity and inflation.
- One of the key mechanisms of transmission in these models operates through the redistribution of income between labor income, capital income and firm's profits.
- If prices are not perfectly flexible, MP tightening should lead to an increase in the markup and a decrease in the income share of labor as prices cannot react immediately to the fall in demand. This effect reduces unit labor costs leading to a downward pressure on inflation.
- For this transmission mechanism to be operative, MP shocks should affect the cyclical behavior of factor income shares in ways that are consistent with these theoretical arguments.

In this Paper

- Despite its importance, studies on the effect of MP shocks on income shares are very limited (e.g. [Christiano et al., 2010], [Ramey, 2016], [Christiano et al., 2016]).
- Our objective is to fill this gap and provide the first cross-country comprehensive study on the effects of monetary policy on the labor share.
- 1. We provide **new and robust evidence** on the effects of **MP shocks** on **the Labor share** for a set of **five** developed economies: The US, the Euro Area, UK, Australia and Canada.
- 2. We compare the empirical results with the **implied transmission mechanism** in standard **DSGE models** displaying nominal, real rigidities and labor market frictions.
 - Given our evidence, are current models used for monetary policy analysis able to match the responses of the variables of interest?

Preview of the Results

- The empirical analysis presents a very robust set of stylized facts: cyclically, a monetary policy tightening *increased* the labor share and *decreased* real wages, and labor productivity.
- These facts are robust across time, across countries, across different Structural Vector Autoregression (SVAR) identification strategies and across sectors.
- These stylized facts are at odds with the responses implied by the standard New Keynesian (NK) model of the business cycle where there is a one to one link between the labor share and marginal costs (mark-up).
- But this mismatch between data and theory is not just a feature of the basic NK model but carries over in richer set ups widely used for MP analysis.

Labor Share, the price mark-up and the Business Cycle

- MP shocks and SVAR evidence: [Christiano et al., 2005], [Olivei and Tenreyro, 2007], [Ramey, 2016], [Basu and House, 2016].
- Labor Share and technology shocks: [Hansen and Prescott, 2005], [Choi and Ríos-Rull, 2009], and [León-Ledesma and Satchi, 2018].
- The cyclicality of mark-ups: [Bils, 1987], [Rotemberg and Woodford, 1999], [Galí et al., 2007], [Hall, 2012], [Nekarda and Ramey, 2013], [Karabarbounis, 2014] and [Bils et al., 2014].
- [Nekarda and Ramey, 2013]: Their conclusions, like ours, cast doubts on the standard transmission mechanism of NK models.
- The conditional correlation of the labor share to demand shocks is still empirically and theoretically an open question.

The transmission mechanism of MP in NK-DSGE models.

- Several mechanisms have been presented that can break down the labor share and the inverse of the mark-up.
 - The Cost channel of Monetary Policy: [Ravenna and Walsh, 2006], [Christiano et al., 2010].
 - Labor market search frictions: [Trigari, 2006], [Christoffel and Kuester, 2008], [Christiano et al., 2016].
 - ► CES production: [Cantore et al., 2014], [Cantore et al., 2015].
 - ► Overtime/Overhead labor: [Bils, 1987], [Nekarda and Ramey, 2013].

Cross Country Labor Share

Data construction and sources



Figure: Cross Country Labor Share

Empirical Analysis: VAR information set - Cholesky

- We consider, as a baseline specification, a 7 variables VAR merging part of the information sets in [Olivei and Tenreyro, 2007] [OT] and [Christiano et al., 2005] [CEE05].
- The variables in the information set are: the log of Real GDP, the log of GDP deflator, the log of an index for price of commodities, log of CPI, log Labor Share, short term interest rates and M2 growth.
- The advantages of using the labor share instead of it's components is that the *composition bias* in the response of real wages and productivity cancels out when one takes their ratio (see [Basu and House, 2016]).

Country	ountry Sample		
US	1984:Q1	2007:Q4	
EA	1999:Q4	2011:Q3	
AUS	1985:Q1	2009:Q4	
CAN	1985:Q1	2011:Q1	
UK	1986:Q1	2008:Q1	

VAR Identification Scheme: Cholesky

normalized 1% increase in the short term interest rate - US

► Full VAR



VAR Robustness: Information Set and Sample

- Using different labor share proxies constructed for the US, Australia and Canada.
- The exact same info sets as in [Olivei and Tenreyro, 2007] and [Christiano et al., 2005].
- Only for the US: the original sample as [CEE05] 1965:Q1-1995Q3 and 1965:Q1-2007:Q4.
- Larger VAR
- Summary

VAR Robustness: Alternative Identification Schemes

- Sign restrictions, as in [Uhlig, 2005].
- External/instrumental variable approach as proposed by [Stock and Watson, 2012] and by [Mertens and Ravn, 2013].



Sectoral Evidence

- Is this evidence robust also across sectors?
- Is the increase in the labor share due to changes in the composition of output from sectors with low to sectors with high labor shares rather than a change of the labor share within sectors?
- We exploit the cross-section and time-series variation of labor shares at the disaggregated sector level.
- Using NBER-CES and Klems data we show that the increase in the LS happens also within sectors.





Labor share components IRFs

- What drives the Labor share responses?
- ► A countercyclical response of the labor share to a monetary policy shock can occur either because real wages are more countercyclical than labor productivity or, vice versa, because labor productivity is more procyclical than real wages. s^h_t = w_t - lp_t
- The two scenarios have very different implications for the transmission mechanism of MP and will prove to be crucial in evaluating the performance of business cycle models.

Labor share components IRFs

- ► We control for different deflators of wages and output ([Pessoa and Van Reenen, 2013]). ► Details
- We check the responses of real wages and labor productivity in the same VAR specifications.
- We find consistently that $s_t^h \uparrow$ because $lp \downarrow > w \downarrow$. Details
- We also control for the *composition bias* discussed before. This makes the response of the *representative agent* real wage (and productivity) more negative than what we find using aggregate data.
- This is in line with the results of: [Christiano et al., 2005] using macro data and [Basu and House, 2016] using micro-data. • Details

Theory

- Are current models of economic fluctuations able to match the response of the labor share, real wages and productivity? And, if so, at which cost?
- ► We check from the simplest version of the NK model, as in [Galí, 2008], to medium scale DSGE models with a broad set of nominal and real frictions ([Christiano et al., 2005], [Christiano et al., 2016]) like the ones currently used for monetary policy analysis.
- ► Given the size of most of these models we do this using a **three step** approach:
 - 1. **Prior Sensitivity Analysis** (PSA): we asses the likelihood of each of the models to generate the sign of LS IRFs consistent with the data, conditional on the model and on a very loose prior specification.
 - 2. **Monte Carlo Filtering** (MCF): to identify the parameters that are able to generate those patterns.
 - Bayesian IRF Matching ([Christiano et al., 2010]): estimate the models (including the parameters identified in step 2) by minimizing the distance between the VAR and DSGE IRFs to a MP shock for a selected number of variables.

Theory: Labor Share in DSGE models

 It is well known that in standard NK models the labor share is equivalent to the inverse of the price markup. [Galí et al., 2007], [Nekarda and Ramey, 2013]

$$\boldsymbol{s}_t^h = \frac{\pi_t - \beta \mathbb{E}_t \pi_{t+1}}{\lambda}$$

- Several mechanisms have been presented that can break down the labor share and the inverse of the mark-up:
 - The Cost channel of Monetary Policy: [Ravenna and Walsh, 2006], [Christiano et al., 2010].
 - Labor market search frictions: [Trigari, 2006], [Christoffel and Kuester, 2008], [Christiano et al., 2016].
 - ► CES production: [Cantore et al., 2014], [Cantore et al., 2015].
 - Overtime/Overhead labor/Fix costs: [Bils, 1987], [Nekarda and Ramey, 2013].



Pool of DSGE Models we compare against the SVAR

- **NK** Medium scale DSGE model with sticky prices and wages + other real rigidities. [Christiano et al., 2005], [Smets and Wouters, 2007]
- NK_CES Medium scale DSGE model + CES production. [Cantore et al., 2014], [Cantore et al., 2015]
- **NK**_**WKN** Medium scale DSGE model + Working capital + firm networks. [Phaneuf et al., 2015].
 - **NK_SM** Medium scale DSGE model with sticky prices and search frictions with Alternating bargaining (no sticky wages). [Christiano et al., 2016]

- Each model has the same Taylor rule $r_t = \rho^r r_{t-1} + (1 - \rho^r) [\rho^{\pi} \pi_t + \rho^{\gamma} y_t] + \varepsilon_t^r$ and the agents information set is consistent with the Cholesky recursive identification of the SVAR.
- We also checked other models like: NK without capital [Galí, 2008], [Galí, 2010]. Sticky Information [Mankiw and Reis, 2007]. Right to manage [Christoffel and Kuester, 2008].

Prior Sensitivity Analysis

- 1 How likely is the structural model to generate the sign pattern of the conditional moments (IRF) we observe in the data?
- As explained by [Canova, 1995], [Lancaster, 2004] and [Geweke, 2005], prior predictive analysis is a powerful tool to shed light on complicated objects that depend on both the joint prior distribution of parameters and the model specification.
- By generating a random sample from the prior distributions, one can compute the reduced form solution and the model-implied statistics of interest, e.g. impulse responses.
- Many replicas of the latter generates an empirical distribution of the model- and prior-implied statistics of interest. ([Leeper et al., 2015] and [Féve and Sahuc, 2014])

Priors

Description	NK	NK_CES	NK.WKN	NK_SM
Inverse of Frish Elasticity of Labor Supply	<i>U</i> [1, 10]	-	U[1, 10]	U[1, 10]
Investment adjustment costs		U[1,	10]	
Habits in Consumption		U[0, 1]		
Variable Capital Utilization		<i>U</i> [0	, 1]	
Calvo price stickiness		<i>U</i> [0, 1]		
Calvo wage stickiness	U[0, 1]	U[0, 1]	U[0, 1]	-
price markup		Ū[1,	1.2]	
wage markup	U[1, 1.2]	U[1, 1.2]	Ū[1, 1.2]	-
Interest rate smoothing		U[0, 1]		
Taylor rule response to inflation		U[1.01, 5]		
Taylor rule response to output	U[0, 1]		, 1]	
Price Indexation	U[0, 1]	U[0, 1]	· ·	-
Wage Indexation	U[0, 1]	U[0, 1]	-	-
K/L elasticity of substitution		U[0.01, 5]	-	-
working capital fraction (labor)	-		U[0, 1]	U[0, 1]
Intermediate inputs share in production	-	-	U[0, 1]	
working capital fraction (capital)	-	-	U[0, 1]	-
working capital fraction (intermediate inputs)	-	-	U[0, 0.7]	-
technology diffusion	-	-		U[0, 1]
prob. of barg. session determination	-	-	-	U[0, 1]
replacement ratio	-	-	-	U[0, 1]
hiring fixed cost relative to output %	-	-	-	U[0, 2]
search cost relative to output %	-	-	-	U[0, 2]
matching function share of unemployment	-	-	-	$U_{[0, 1]}$
job survival rate	-	-	-	U[0, 1]
vacancy filling rate	-	-	-	<i>U</i> [0, 1]

Uniform Distribution bounds for PSA and MCF.

Prior Sensitivity Analysis

We check the % of the parameter space that generates a (+) IRF of labor share and a (-) IRF of wages and labor productivity from quarters 2 to 5 and 5 to 8.

	Restrictions			
	2:5 quarters		5:8 quarters	
Model	ls (+)	ls (+); lp (-); w (-)	ls (+)	ls (+); lp (-); w (-)
NK	30.9%		59.7%	
NK_CES	11.2%		55.1%	
NK_WKN	26.5%		54.4%	
NK_SM	6.2%		46.0%	

Prior Sensitivity Analysis

We check the % of the parameter space that generates a (+) IRF of labor share and a (-) IRF of wages and labor productivity from quarters 2 to 5 and 5 to 8.

	Restrictions				
	2	2:5 quarters	5:8 quarters		
Model	ls (+)	ls (+); lp (-); w (-)	ls (+)	ls (+); lp (-); w (-)	
NK	30.9%	1.7%	59.7%	13.9%	
NK_CES	11.2%	0.7%	55.1%	4.6%	
NK_WKN	26.5%	9.2%	54.4%	13.3%	
NK_SM	6.2%	2.8%	46.0%	13.5%	

Monte carlo filtering methods

- 2 Which are the parameters that mostly drive these patterns in each model?
- This question is more subtle because it requires an inverse mapping. Montecarlo filtering (MCF) techniques offer a statistical framework to tackle this question.
- MCF are computational tools that allow researchers to recover, in a nonlinear model, the critical inputs that generate a particular model output.
- ► In MCF all parameters move simultaneously.
- Smirnoff test offers implicitly a statistical ranking of parameters from the most to the least influential ones.

MCF: Parameters driving prior restrictions in each model.

Description	NK	NK_CES	NK_WKN	NK_SM
Relative Risk Aversion				
Inverse of Frish Elasticity of Labor Supply				
Investment adjustment costs	<u> </u>	×.	×.	✓
Habits in Consumption		✓	\checkmark	
Variable Capital Utilization				
Calvo price stickiness	<u> </u>	<u> </u>	<u>×</u>	
Calvo wage stickiness	~	✓	<u>×</u>	
price markup	✓		<u> </u>	<u> </u>
wage markup				
Interest rate smoothing	✓	×	<u> </u>	
Taylor rule response to inflation				
Taylor rule response to output				
Price Indexation				
Wage Indexation		/		
K/L elasticity of substitution		~	/	-
working capital fraction (labor)			~	<u> </u>
merhediate inputs share in production			<u> </u>	
working capital fraction (intermediate inputs)				
tochnology diffusion				
prob of barg spesion determination				
replacement ratio				1
hiring fixed cost relative to output %				<u>×</u>
search cost relative to output %				
matching function share of unemployment				1
iob survival rate				<u>.</u>
vacancy filling rate				<u> </u>

Parameters responsible for matching prior restrictions over quarters 2:5 (black checkmark), 5:8 (red checkmark) and 2:8 (red underlined checkmark).

Bayesian IRF Matching

- ► We partition each model parameters into two groups. The first is composed of **calibrated** ones.
- The second group of parameters, for each model, is estimated by minimizing a measure of the distance between the models and empirical impulse response functions.

details

 Follow [Christiano et al., 2005], [Christiano et al., 2010] and [Christiano et al., 2016] we use a Limited information Bayesian approach.

IRF Matching: 11 Variables SVAR - US 59Q2:08Q4

 Y_t

11*x*1

►

 Combine our baseline Cholesky specification with the three different price indices with the specification of [Altig et al., 2011].

$$\int_{A} \left[\begin{array}{c} \Delta ln(relative price of investment_{t}) \\ \Delta ln(GDP_{t}) \\ \Delta ln(GDP deflator_{t}) \\ \Delta ln(price of commodities_{t}) \\ \Delta ln(CPl_{t}) \\ Capacity Utilization_{t} \\ \Delta ln(Consumption_{t}) \\ \Delta ln(Investment_{t}) \\ ln(Labor Share_{t}) \\ Federal Funds Rate_{t} \\ \Delta M2_{t} \end{array} \right]$$

(1)

.

IRF Matching: 11 Variables SVAR - US 59Q2:08Q4



IRF Matching: 11 Variables SVAR - US 59Q2:08Q4

GDP Inflation **Federal Funds Rate** 0.8 0.4 -0.2 -0.2 0 -0.4 5 10 5 10 5 10 0 0 Consumption Investment **Capacity Utilization** 0 0 0 -0.2 -1 -0.8 5 10 0 5 10 0 5 10 0 Labor Share 0.2 0.1 5 10 0 VAR 68% VAR Mean NK -----NK CES NK WKN NK SM

Conclusions

- We shed some light on the effect of monetary policy on factor shares and their components: key transmission mechanism of MP in NK models.
- We present a robust set of stylized facts: cyclically, a monetary policy tightening (easing) increased (decreased) the labor share and decreased (increased) real wages and labor productivity.
- We show that this is at odds with the theoretical transmission mechanism of monetary policy in structural models widely used for policy analysis.
- Models that can do a reasonable job at reproducing the dynamic responses of real variables cannot simultaneously match the dynamics of the labor share.

Conclusions

- Our results emphasise the need to develop model extensions able to replicate the cyclical behaviour of the labor share and its components.
- So far, neither models with price or/and wage rigidities and other relevant real frictions are able to match the dynamics observed in the data, casting doubts on the traditional theoretical transmission mechanism attributed to MP.
- This suggest that serious models of joint profit and wage determination, or models with firm and worker heterogeneity where markups and wages display pro-cyclical patterns appear as promising potential avenues for research.

Appendix

Data Construction and Sources: Labor Share

- Measuring the share of labor in total income is complicated by problems associated with how to impute certain categories of income to labor and capital owners.
- The existence of self-employment income, the treatment of the government sector, the role of indirect taxes and subsidies, household income accruing from owner occupied housing, and the treatment of capital depreciation, are common problems highlighted in the literature.
- These have been discussed at length in [Gollin, 2002]), [Gomme and Rupert, 2004] and more recently in [Muck et al., 2015].
- ► We use 7 different proxies of Labor share for the US.

Data Construction and Sources: US Labor Share - 7 measures

- LS1 An index of the Labor Share in the Non-Farm Business Sector taken from BLS.
- LS2 Labor share in the domestic corporate non-financial business sector as discussed by GR07. (*No issues with proprietors income and rental income, two ambiguous components of factor income.*)
- LS3 Deals with imputing ambiguous income (AI) and corresponds to the second alternative measure of the labor share proposed in GR07. The measure excludes the household and government sectors.
- LS4 Same as the above LS3 but not corrected for inventory valuation adjustment and an adjustment for capital consumption.
- LS5 Deals with AI as in [Ríos-Rull and Santaeulália-Llopis, 2010] in the calculation of the capital share.
- LS6 Taken from [Fernald, 2014]. In computing the capital share assumes non-corporate sector has the same factor shares as the corporate non-financial sector.
- LS7 An index of the Labor Share in the Non-Financial Corporation Sector taken from BLS.



Data Construction and Sources: Labor Share

▶ return

- We constructed measures of the labor share on a quarterly basis for some other countries for which data were available for a sufficiently long period of time.
- Those countries are Australia (1959:Q3-2016:Q1), Canada (1980:Q2-2016:Q1), the Euro Area (1980:Q1-2014:Q4) and the UK (1955:Q1-2016:Q1).
- ► For some of these countries, however, data availability limits the extent to which we can obtain corrected labor share measures and, in many cases, we work with rough estimates of labor shares.
- We use one each for the Euro Area and the UK, 2 for Canada and 5 for Australia.

Data on Wages and Labor Productivity

US Proxies



AUS Proxies



CAN Proxies


Data Construction and Sources: Wages and Labor Productivity

- For real wages, we used nominal compensation of employees deflated by the CPI over hours worked from the Valery Ramey database and [Ohanian and Raffo, 2012].
- Labor productivity is calculated as real GDP over hours worked from the same databases.

▶ return

1 Labor share 1: Labor share in the non-farm business sector. This is taken directly from BLS. The series considers only the non-farm business sector. It calculates the labor share as compensation of employees of the non-farm business sector plus imputed self-employment income over gross value added of the non-farm business sector. Self-employment imputed income is calculated as follows: an implicit wage is calculated as compensation over hours worked and then the imputed labor income is the implicit wage times the number of hours worked by the self-employed.

return

2 Labor share 2: Labor share in the domestic corporate non-financial business sector. This follows [Gomme and Rupert, 2004] first alternative measure of the labor share. The use of data for the non-financial corporate sector only has the advantage of not having to apportion proprietors income and rental income, two ambiguous components of factor income. It also considers the wedge introduced between the labor share and one minus the capital share by indirect taxes (net of subsidies), and only makes use of unambiguous components of capital income. This approach also takes into account the definition of aggregate output in constructing the labor share. In all the above measures we used GDP, however sectoral studies often use gross value added (GVA) (see [Bentolila and Saint-Paul, 2003], [Young, 2010] and [Young, 2013]). [Valentinyi and Herrendorf, 2008] and [Muck et al., 2015] show that factor shares in value added differ systematically from factor income shares in GDP. By considering gross value added net interest and miscellaneous payments (Nl_t^{gva} , NIPA Table 1.14), gross value added corporate profits (CP_{t}^{gva} , NIPA Table 1.14), net value added (NVA, NIPA Table 1.14) and gross value added taxes on production and imports less subsidies (Tax_t^{gva} , NIPA Table 1.14) the labor share is thus calculated as:

Labor Share 2:
$$LS_t = 1 - \frac{CP_t^{gva} + NI_t^{gva} - Tax_t^{gva}}{NVA_t}$$
.

return

3 *Labor share 3*: This approach deals with imputing ambiguous income for the macroeconomy and corresponds to the second alternative measure of the labor share proposed in [Gomme and Rupert, 2004]. The measure excludes the household and government sectors. They define unambiguous labor income (Y^{UL}) as compensation of employees, and unambiguous capital income (Y^{UK}) as corporate profits, rental income, net interest income, and depreciation (same series as above from NIPA Tables 1.1.12 and 1.7.5). The remaining (ambiguous) components are then proprietors' income plus indirect taxes net of subsidies (NIPA Table 1.1.12). These are apportioned to capital and labor in the same proportion as the unambiguous components. The resulting labor share measure is:

Labor Share 3:
$$LS_t = \frac{CE_t}{CE_t + RI_t + CP_t + NI_t + \delta_t} = \frac{Y^{UL}}{Y^{UK} + Y^{UL}}.$$

▶ return

4 **Labor share 4**: This is the same as the above Labor Share 3 but not corrected for inventory valuation adjustment and an adjustment for capital consumption. Using rental income of persons (without CCAdj) (Rl_t^a , NIPA Table 1.1.12) and corporate profits before tax (without IVA and CCAdj) (CP_t^a , NIPA Table 1.1.12):

Labor Share 4:
$$LS_t = \frac{CE_t}{CE_t + RI_t^a + CP_t^a + NI_t + \delta_t} = \frac{Y^{UL}}{Y^{UK} + Y^{UL}}$$

▶ return

5 *Labor share 5*: Follows [Ríos-Rull and Santaeulália-Llopis, 2010] and is similar to *PI-2-GDP*. The labor share of income is defined as one minus capital income divided by output. As above, to deal with mixed income, they assume that the proportion of ambiguous capital income to ambiguous income is the same as the proportion of unambiguous capital income to unambiguous income. But the calculation somewhat differ in the computation of Unambiguous income and in the use of Gross National Product (*GNP*_t, NIPA Table 1.7.5) instead of GDP.

$$CS_{t}^{U} = \frac{UCI_{t} + \delta_{t}}{UI_{t}} = \frac{RI_{t} + NI_{t} + GE_{t} + CP_{t} + \delta_{t}}{RI_{t} + NI_{t} + GE_{t} + CP_{t} + \delta_{t} + CE_{t}}$$
$$ACI_{t} = CS_{t}^{U}AI_{t}$$
Labor Share 5: $LS_{t} = 1 - CS_{t} = 1 - \frac{UCI_{t} + \delta_{t} + ACI_{t}}{GNP_{t}}$

- 6 *Labor share 6*: Is taken from [Fernald, 2014] and it's utilization adjusted quarterly series. In computing the capital share he assumes that the non-corporate sector has the same factor shares as the corporate non-financial sector. But it's not exactly the same implementation as in *Labor Share 2*.One difference, for example, is in the treatment of some taxes on production and imports that represents payments for capital, namely property taxes and motor vehicle taxes.
- 7 *Labor share 7*: Labor share in the non-finanical corporation sector. This is taken directly from BLS (FRED series id PRS88003173 provided as an index number). The series considers only the non-finanical corporations sector.

Data Construction and Sources: Australia 1959:Q3-2016:Q1 Source: Australian Bureau of Statistics

- 1. Total wages and salaries (including social security contributions) over GDP (AUS_LS1).
- 2. Total wages and salaries (including social security contributions) over total factor income (AUS_LS2).
- 3. One minus gross operating surplus of private non-financial corporations as a percentage of total factor income (AUS_LS3).
- 4. One minus gross operating surplus of private non-financial corporations plus all financial corporations as a percentage of total factor income (AUS_LS4).
- (total income surplus of all corporations gross operating surplus of government - mixed income imputed to capital)/total income (AUS_LS5).

Data Construction and Sources: Canada 1980:Q2-2016:Q1 Source: Statistics Canada

- 1. Compensation of employees over total factor income (GDP corrected by taxes and subsidies) (CAN_LS1).
- We imputed mixed income in the same proportion as unambiguous labor and capital income, and added it to the previous measure of labor income (CAN_LS2).

Data Construction and Sources: UK, and EA

- UK Compensation of employees over gross value added at factor costs (UK_LS). (1955:Q1-2013:Q3 from the Office for National Statistics).
- EA Compensation of employees over GDP at factor costs (EA_LS). (1999:Q1-2013:Q4 period from the Area Wide Model database).

Descriptive Statistics

return

Country	Sample	LS	W	LP
US	1955Q1-2015Q3	[-0.29 , 0.04]	[0.13 , 0.47]	[0.14 , 0.50]
EA	1999Q1-2014Q4	[-0.91 , -0.37]	[-0.34 , 0.46]	[0.84 , 0.95]
UK	1971Q1-2016Q1	[-0.41, 0.11]	[-0.26 , 0.19]	[0.19 0.64]
AUS	1959Q3-2013Q4	[-0.23, 0.12]	[-0.35, -0.01]	[0.13, 0.43]
CAN	1981Q2-2013Q4	[-0.56 , -0.07]	[-0.49 , -0.04]	[0.16 , 0.47]

Table: Correlation with HP filtered Output. GMM 95 % Confidence Intervals. Wages and Labor productivity are HP filtered

Descriptive Statistics

return

Country	Sample	LS	W	LP
US	1955Q1-2015Q3	[0.28 , 0.60]	[-0.51 , -0.12]	[-0.55 , -0.19]
EA	1999Q1-2014Q4	[-0.76 , -0.28]	[-0.92 , -0.58]	[-0.85 , -0.18]
UK	1971Q1-2016Q1	[-0.52, 0.08]	[-0.90 , -0.79]	[-0.94 , -0.82]
AUS	1959Q3-2013Q4	[0.49, 0.70]	[-0.67 , -0.36]	[-0.68 , -0.38]
CAN	1981Q2-2013Q4	[0.45 , 0.72]	[-0.91 , -0.82]	[-0.92 , -0.85]

Table: Correlation with the policy rate. GMM 95 % Confidence Intervals. Wages and Labor productivity are HP filtered.

return

	Mean	Median	Std₋Dev
LS1	0.74	0.75	0.03
LS2	0.72	0.72	0.02
LS3	0.71	0.71	0.02
LS4	0.71	0.71	0.02
LS5	0.65	0.65	0.02
LS6	0.67	0.68	0.02
LS7	0.73	0.74	0.03
W	0.00	-0.01	0.15
LP	0.00	0.00	0.28

return

	LS1	LS2	LS3	LS4	LS5	LS6	LS7	W	LP
LS1	1.00	0.41	0.89	0.87	0.87	0.91	0.87	-0.78	-0.82
LS2	0.41	1.00	0.33	0.30	0.34	0.64	0.75	0.11	0.10
LS3	0.89	0.33	1.00	0.93	0.99	0.88	0.82	-0.68	-0.79
LS4	0.87	0.30	0.93	1.00	0.93	0.85	0.79	-0.72	-0.78
LS5	0.87	0.34	0.99	0.93	1.00	0.88	0.83	-0.63	-0.76
LS6	0.91	0.64	0.88	0.85	0.88	1.00	0.97	-0.59	-0.65
LS7	0.87	0.75	0.82	0.79	0.83	0.97	1.00	-0.50	-0.56
W	-0.78	0.11	-0.68	-0.72	-0.63	-0.59	-0.50	1.00	0.96
LP	-0.82	0.10	-0.79	-0.78	-0.76	-0.65	-0.56	0.96	1.00

Table: Correlations

return

	Bootstrapped		GMM		
	ub	lb	ub	lb	
LS1	-0.166	0.067	-0.234	0.125	
LS2	-0.221	-0.013	-0.289	0.043	
LS3	-0.176	0.051	-0.249	0.122	
LS4	-0.219	-0.008	-0.284	0.054	
LS5	-0.135	0.099	-0.214	0.173	
LS6	-0.130	0.081	-0.192	0.146	
LS7	-0.128	0.090	-0.190	0.151	
W	0.176	0.407	0.129	0.469	
LP	0.178	0.435	0.140	0.497	

Table: 95% Confidence Intervals for correlation with Output (HP Filtered). Wages and Labor productivity are also HP filtered.

return

	Bootstrapped		GMM	
	ub	lb	ub	lb
LS1	0.423	0.614	0.365	0.680
LS2	0.341	0.543	0.283	0.596
LS3	0.220	0.448	0.152	0.530
LS4	0.105	0.353	0.022	0.444
LS5	0.222	0.450	0.152	0.534
LS6	0.493	0.653	0.448	0.703
LS7	0.527	0.680	0.477	0.724
W	-0.445	-0.201	-0.510	-0.125
LP	-0.486	-0.267	-0.546	-0.195

Table: 95% Confidence Intervals for correlation with Fed Funds Rates (Raw)

return

	Mean	Median	Std_Dev
LS1	0.50	0.49	0.03
LS2	0.56	0.55	0.03
LS3	0.83	0.83	0.02
LS4	0.79	0.80	0.03
LS5	0.70	0.70	0.03
W	0.00	-0.04	0.35
LP	0.00	-0.02	0.40

return

	LS1	LS2	LS3	LS4	LS5	W	LP
LS1	1.00	0.97	0.78	0.86	0.97	-0.75	-0.80
LS2	0.97	1.00	0.82	0.85	0.95	-0.64	-0.71
LS3	0.78	0.82	1.00	0.93	0.85	-0.72	-0.75
LS4	0.86	0.85	0.93	1.00	0.93	-0.88	-0.90
LS5	0.97	0.95	0.85	0.93	1.00	-0.80	-0.85
W	-0.75	-0.64	-0.72	-0.88	-0.80	1.00	1.00
LP	-0.80	-0.71	-0.75	-0.90	-0.85	1.00	1.00

Table: Correlations

▶ return

	Bootstrapped		GMM	
	ub	lb	ub	lb
LS1	-0.263	0.029	-0.301	0.076
LS2	-0.296	0.009	-0.345	0.063
LS3	-0.235	0.015	-0.284	0.052
LS4	-0.182	0.076	-0.233	0.118
LS5	-0.210	0.068	-0.253	0.118
W	-0.302	-0.023	-0.342	-0.009
LP	0.171	0.400	0.132	0.433

 Table:
 95% Confidence Intervals for correlation with Output (HP Filtered).
 Wages and Labor Productivity are also HP Filtered.

▶ return

	Bootstrapped		GMM	
	ub	lb	ub	lb
LS1	0.352	0.563	0.287	0.629
LS2	0.380	0.597	0.317	0.665
LS3	0.332	0.511	0.270	0.570
LS4	0.533	0.661	0.492	0.702
LS5	0.413	0.603	0.358	0.662
W	-0.610	-0.424	-0.675	-0.363
LP	-0.615	-0.436	-0.677	-0.376

Table: 95% Confidence Intervals for correlation with Short term interest rates (Raw)

return

	Mean	Median	Std_Dev
LS1	0.55	0.55	0.02
LS2	0.62	0.62	0.03
W	0.00	-0.03	0.19
LP	0.00	-0.01	0.22

	LS1	LS2	W	LP
LS1	1.00	0.97	-0.61	-0.69
LS2	0.97	1.00	-0.65	-0.71
W	-0.61	-0.65	1.00	0.99
LP	-0.69	-0.71	0.99	1.00

Table: Correlations



	Bootstrapped		GMM	
	ub	lb	ub	lb
LS1	-0.408	-0.066	-0.521	0.031
LS2	-0.453	-0.141	-0.558	-0.070
W	-0.425	-0.092	-0.492	-0.038
LP	0.183	0.431	0.157	0.474

 Table:
 95% Confidence Intervals for correlation with Output (HP Filtered).
 Wages and Labor Productivity are also HP Filtered.

	Bootstrapped		GMM	
	ub	lb	ub	lb
LS1	0.523	0.709	0.477	0.767
LS2	0.502	0.672	0.453	0.723
W	-0.891	-0.838	-0.906	-0.822
LP	-0.911	-0.865	-0.923	-0.851

Table: 95% Confidence Intervals for correlation with Short term interest rates (Raw)

Descriptive Stats EA

▶ return

	Mean	Median	Std_Dev
LS	0.47	0.48	0.01
W	0.00	-0.01	0.03
LP	0.00	0.00	0.03

	LS	W	LP
LS	1.00	0.41	-0.13
W	0.41	1.00	0.85
LP	-0.13	0.85	1.00

Table: Correlations

Descriptive Stats EA

▶ return

	Bootstrapped		GN	ЛМ
LS	-0.773	-0.412	-0.907	-0.375
W	-0.233	0.351	-0.339	0.460
LP	0.842	0.934	0.839	0.950

 Table:
 95% Confidence Intervals for correlation with Output (HP Filtered).
 Wages and Labor Productivity are also HP filtered.

	Bootstrapped		GMM	
	ub	lb	ub	lb
LS	-0.663	-0.367	-0.759	-0.283
W	-0.847	-0.618	-0.918	-0.573
LP	-0.705	-0.302	-0.848	-0.179

Table: 95% Confidence Intervals for correlation with Short term interest rates (Raw)

Descriptive Stats UK

▶ return

	Mean	Median	Std_Dev
LS	0.56	0.56	0.03
W	0.00	-0.05	0.25
LP	0.00	0.02	0.21

	LS	W	LP
LS	1.00	0.34	0.15
W	0.30	1.00	0.98
LP	0.15	0.98	1.00

Table: Correlations

Descriptive Stats UK

▶ return

	Bootstrapped		GN	1M
LS	-0.303	0.018	-0.415	0.115
W	-0.195	0.135	-0.260	0.196
LP	0.243	0.559	0.195	0.638

 Table:
 95% Confidence Intervals for correlation with Output (HP Filtered).
 Wages and Labor Productivity are also HP filtered.

	Bootstrapped		GMM	
	ub	lb	ub	lb
LS	-0.411	-0.046	-0.519	0.077
W	-0.881	-0.814	-0.903	-0.795
LP	-0.913	-0.838	-0.936	-0.823

Table: 95% Confidence Intervals for correlation with Short term interest rates (Raw)

VAR Data details: US

return

- CPI: CPI of all good for all urban consumers for US.
- Real GDP all Economy.
- ► GDP Deflator.
- ► Price of commodity index: CBR SPOT commodity index.
- M2 from IMF.
- Federal Funds Rates
- Real wages: we used nominal compensation of employees deflated by the CPI over hours worked from the Valery Ramey database.
- Labor productivity is calculated as real GDP over hours worked from the same databases.

VAR Data details: EA

- ► Price of commodity index: CBR SPOT commodity index.
- ► We consider the OECD and New AWM database.
- HICP excluding energy
- Short-term interest rate
- ► real GDP
- ► the GDP deflator
- M2 from IMF.
- For Real wages: compensation of employees from OECD QNA deflated by CPI and total hours from AWM.
- ► For Labor productivity we use Real GDP over total hours.
- ► All variables are in logs but short term interest rate.

VAR Data details: AUS, CAN and UK

return

- ► For core CPI we used OECD consumer prices of all goods.
- ► Price of commodity index: CBR SPOT commodity index.
- For real consumption expenditure we used real private final consumption expenditure from the OECD.
- ► For real investment we used real gross fixed capital formation from the OECD.
- Short term interest rates
- M2 from datastream
- For Real wages: compensation of employees from OECD QNA deflated by CPI and total hours from [Ohanian and Raffo, 2012].
- ► For Labor productivity we use Real GDP over total hours.

normalized 1% increase in the short term interest rate



normalized 1% increase in the short term interest rate - UK

return



normalized 1% increase in the short term interest rate - AUS



normalized 1% increase in the short term interest rate - CAN



normalized 1% increase in the short term interest rate - EA

return



VAR Robustness - Cholesky US different proxies

normalized 1% increase in the short term interest rate. 1984Q1-2007Q4 V return





VAR Robustness - Cholesky AUS different proxies

normalized 1% increase in the short term interest rate.


VAR Robustness - Cholesky CAN different proxies



VAR Robustness - Cholesky US Sample 1965Q3-1995Q3



VAR Robustness - Cholesky US Sample 1965Q3-2007Q4



VAR Robustness - Cholesky US - 9 variable VAR





VAR Robustness - Cholesky summary

return

Country	Info set	Sample	LS + reponse
	Baseline		ALL Proxies
	CEE05	84-07	ALL Proxies
	OT		ALL Proxies
	Baseline		ALL Proxies
US	CEE05	65-95	ALL Proxies
	OT		ALL Proxies
	Baseline		ALL Proxies
	CEE05	65-07	All except LS6
	OT I		ALL Proxies
EA	Baseline		Yes
	CEE05	99-11	Yes
	OT		Yes
UK	Baseline		Yes
	CEE05	86-08	No
	OT I		Yes
AUS	Baseline		ALL Proxies
	CEE05	85-09	ALL Proxies except LS3
	OT		ALL Proxies
CÁN	Baseline		ALL Proxies
	CEE05	85-11	ALL Proxies
	I OT		ALL Proxies

Table: VAR Cholesky robustness

VAR Robustness: Alternative Identification Schemes

return

- Sign restrictions, see [Uhlig, 2005]. We postulate that a monetary policy shock
 - increases the short term nominal interest rate at t = 0, 1, 2
 - decreases prices, i.e. the GDP deflator and CPI at t = 0, 1, 2
 - ▶ induces a contraction in M2 at t = 0, 1, 2

VAR Results: Robustness - Sign Restrictions



VAR Robustness: Alternative Identification Schemes

▶ return

- ► Using the external/instrumental variable approach as proposed by [Stock and Watson, 2012] and by [Mertens and Ravn, 2013].
 - The monetary policy shock in the structural VAR is identified as the predicted value in the population regression of the instrument on the reduced form VAR residuals.
 - For this result to hold, the instrument needs to be valid; that is it needs to be relevant (correlated with the unobserved monetary policy shock of the VAR) and exogenous (uncorrelated with the other shocks).
 - We use 5 different proxy or instruments for monetary policy surprises for the US.

VAR Results: Robustness - External Instrument

▶ return

R&R [Romer and Romer, 2004] narrative measure of monetary policy.

- GSS The 'target' factor of [Gürkaynak et al., 2005], which measures surprise changes in the target federal funds rate (quarterly sums of daily data, 1990Q1-2004Q4).
 - SW Estimated monetary policy innovations in the [Smets and Wouters, 2007] model and spans the period 1959q1-2004q4.
- G&K [Gertler and Karadi, 2015] measure of monetary policy surprise and spans the period 1991q1 - 2012q4. It is constructed as the surprise of the current federal funds rate within a 30 minutes window of the FOMC announcement.
- MIR The component in market-based monetary surprises that is orthogonal to the central bank's forecasts about the current and future economic outlook. [Miranda-Agrippino, 2016], [Miranda-Agrippino and Ricco, 2017]

VAR Results: Robustness - External Instrument



Sectoral Evidence: Panel model

return

We can estimate the impact of the shock on sectoral labor shares by running the following panel model:

$$S_{i,t}^{h} = \alpha_{i} + \alpha_{t} + \rho S_{i,t-1}^{h} + \theta M P_{t} + \epsilon_{i,t},$$
(2)

- where α_i and α_t are sector and time-specific fixed effects, and $\epsilon_{i,t}$ is an error term.
- θ then captures the contemporaneous effect of the MP shock on the labor share controlling for past values of the labor share as well as sector and time fixed effects.
- To capture the effect of the MP shock on the labor share after the shock, we estimate:

$$S_{i,t+h}^{h} = \alpha_{i} + \alpha_{t+h} + \rho S_{i,t+h-1}^{h} + \theta_{h} M P_{t} + \epsilon_{i,t+h}.$$
(3)

with h = 1, 2, 3, 4.

• Coefficient θ_h then captures the effect of the MP shock at time *t* on the labor share t + h periods ahead.

Sectoral Evidence: Data

- ► Two databases:
 - NBER-CES productivity database: highly disaggregated split of the US manufacturing sector (464 sectors - 1985-2007).
 - Klems database: less disaggregated split by sectors but covers not only manufacturing but all sectors in the economy including services (30 sectors -1987-2007).
- The labor share at the sector level is defined as compensation of employees over value added.
- ► The measure of *MP*^t is obtained by aggregating quarterly shocks from the Cholesky SVAR using aggregate data.
- Standard errors are estimated following Driscoll and Kraay (1998).



Sectoral Evidence: NBER - Cholesky VAR MP

return



Figure: Coefficient on monetary policy shock variable (Cholesky VAR) using the NBER manufacturing database (464 manufacturing sectors). Period is 1985-2007. The plot shows the coefficient on the year of impact (t_1) and four years after.

Sectoral Evidence: NBER - Romer and Romer VAR MP



Figure: Coefficient on monetary policy shock variable (Romer and Romer) using the NBER manufacturing database (464 manufacturing sectors). Period is 1985-2007. The plot shows the coefficient on the year of impact (t_1) and four years after.

Sectoral Evidence: Klems - Cholesky VAR MP

return



Figure: Coefficient on monetary policy shock variable (Cholesky VAR) using the Klems database (30 sectors). Period is 1987-2007. The plot shows the coefficient on the year of impact (t_1) and four years after.

Sectoral Evidence

return



Figure: Average and dispersion of (log) labor shares in the NBER productivity database, 1985-2007.

Labor share components and the deflators

▶ return

- In the data, real wages are usually deflated using a different price index (typically CPI) from the one of income or GDP (see [Pessoa and Van Reenen, 2013]).
- ► Labor share is defined as the ratio between real hourly compensation (W') and labor productivity (LP) which is the ratio between real GDP deflated using the GDP deflator and a measure of hours:



► In most the theory models, instead, *W^r* and *LP* have, by construction, the same deflators and we need take this into account when comparing empirical and theoretical IRFs.

▶ return

- For the US now we use data for the non-financial corporate sector only in the VAR.
- ► We use the same Choleski identification assumption as before and we run a VAR under two different information sets.
 - 1 A 8 variable set that augments the baseline 7 variable VAR by substituting the labor share with (the log of) real wages and labor productivity.
 - 2 We substitute labor productivity with hours worked.

Labor share components IRFs

return



▶ return

- We argued that one of the advantages of using the labor share is that the *composition bias* in the response of real wages and productivity is alleviated when one takes their ratio as argued by [Basu and House, 2016].
- It can be shown that if anything the composition bias would work in favour of our evidence thus making the response of the representative agent real wage (and productivity) more negative than what we find using aggregate data.

Details - composition bias adjusted data

- We simplify the argument in [Basu and House, 2016], abstracting from entry and exit of new workers and matching quality.
- ► Calling x_t our measure of aggregate labor productivity or real hourly wages (w^r_t, LP_t).
- ► Assume we can classify workers in a discreet grid of N levels of "human capital" or skills from lowest to highest, j = 1,..., N.
- Then, aggregate productivity or wages are simply the weighted sum by level of human capital: x_t = ∑_j x_{j,t}α_{j,t} where α_{j,t} is the weight of hours worked by workers of human capital level *j* in total hours worked (α_{j,t} = H_{j,t}/∑_j H_{j,t}).
- ► We can decompose that measure in two terms:

$$\mathbf{x}_{t} = \sum_{j} \mathbf{x}_{j,t} \alpha_{j,t} = \overline{\mathbf{x}}_{t} + \sum_{j} (\mathbf{x}_{j,t} - \overline{\mathbf{x}}_{t}) (\alpha_{j,t} - \overline{\alpha}_{t}) = \underbrace{\mu_{t}}_{\text{un-weighted average}} + \underbrace{\theta_{t}}_{\text{covariance}},$$

where \overline{x}_t and $\overline{\alpha}_t$ are the averages of wages/productivity and the shares of workers of different levels of human capital respectively.

- μ_t is the wage/productivity of the "representative" worker.
- θ_t tells us about the structure of the labor force: whether shares are increasing or decreasing in productivity (the skill-composition). Changes in this term would precisely be related to the composition bias.
- Our interest is in the cyclical evolution of μ_t conditional on a MP tightening, since this is the direct correspondence between data and models in a large class of representative agent DSGEs.
- ► Call f(., t)_{MP} the impulse response function (IRF) over t = 1,..., T of any variable to a MP tightening.
- $f(x_t, t)_{MP} = f(\mu_t, t)_{MP} + f(\theta_t, t)_{MP} \forall t.$
- Suppose, for simplicity, $f(x_t, t)_{MP} = 0 \forall t$.
- This implies that: $f(\mu_t, t)_{MP} = -f(\theta_t, t)_{MP}$.

- Suppose we know that, in an expansion, the share of low skilled workers increases and it falls in a recession as discussed in [Basu and House, 2016].
- Thus, the change in this covariance is negative during an expansion. [Basu and House, 2016] also show that, conditional on a MP shock, the composition bias changes: the covariance increases (falls) with a MP tightening (loosening).
- It immediately follows then that, if the aggregate response is zero, then the "representative worker" response must be negative with a MP tightening.
- Our findings above show that the response of aggregate labor productivity is negative and aggregate real wages respond *at least* non-positively (and negatively in most cases).
- From the above argument, the response of the representative agent wage/productivity would then be negative. That is, it will be more negative than the one obtained using aggregate data.

Labor share components IRFs

▶ return

- Here we present results using the same baseline cholesky specification substituting the labor share in turn with data on aggregate wages in the US and composition bias corrected measures of wage as constructed by [Haefke et al., 2013].
- ► The sample is 1984-2006 as their datasets stops in 2006.

Labor share components IRFs

return



Theory: Simple NK model

▶ return

$$\bullet \ s_t^h = w_t + h_t - y_t$$

• Assuming monopolistic competition in production, Calvo price stickiness and competitive labor market: $w_t = \theta_t + y_t - h_t$

real marginal costs labor productivity

 $\blacktriangleright \rightarrow \mathbf{s}_t^h = \theta_t = \frac{\pi_t - \beta \mathbb{E}_t \pi_{t+1}}{\lambda}$

- ► A temporary decline in inflation (tighter MP) will see marginal costs (*labor share*) decline and mark-up increase.
- This result is independent of: factor adjustment costs, nominal wage rigidities, financial frictions.
- The result above is true in an economy with or without capital accumulation provided that the production function is either Cobb-Douglas or linear in labor.
- Furthermore if we assume for simplicity $y_t = h_t \Rightarrow w_t = s_t^h = \theta_t$.

Theory: The cost channel of Monetary policy

▶ return

- ► The cost-push channel, of, e.g. [Ravenna and Walsh, 2006], introduces a direct effect of the interest rate on the marginal cost w_t = θ_t + y_t - h_t - rn_t
- This implies $s_t^h = \theta_t rn_t$ This implies $s_t^h = \theta_t \Uparrow rn_t \Downarrow$
- Nominal interest rate *rnt* moves counter-cyclically, therefore it reinforces the pro-cyclicality of the labour share.
- This channel is able to reproduce a pro-cyclical movement of the price mark-up following a monetary policy shock but it is not able to reproduce the counter-cyclicality of the labor share because Δ*rn* > Δθ if monetary policy satisfies the taylor principle.

Theory: CES production function

▶ return

 [Galí et al., 2007] and [Nekarda and Ramey, 2013] show that the CES production function provides a simple way of introducing a wedge between the labor share and the marginal costs:

►
$$s_t^h = \theta_t + \frac{1-\sigma}{\sigma}(y_t - h_t), s_t^h = \theta_t \Downarrow + \underbrace{\frac{1-\sigma}{\sigma}(y_t - h_t)}_{\text{if } \sigma > 1} \Uparrow$$

- where σ is the elasticity of substitution between capital and labor.
- For any reasonable parameterization, the reaction of θ_t to an MP shock always dominates, and the CES assumption does not change significantly the reaction of the labor share, which is always strongly correlated with θ_t.

Theory: Fixed/Overhead Costs

▶ return

- $Y_t = H_t F$ in levels
- $y_t = h_t(1 + \frac{F}{Y})$ in log-linear deviations
- $w_t = \theta_t$ but now $s_t^h = w_t h_t + y_t = \theta_t h_t + h_t (1 + \frac{F}{Y})$

$$\blacktriangleright \Rightarrow \mathbf{s}_t^h = \theta_t - h_t \frac{F}{Y} \mathbf{s}_t^h = \theta_t \Downarrow - h_t \frac{F}{Y} \Uparrow$$

- Given that hours (output) responds procyclically to a MP shock then the higher ^F/_V the higher the wedge between labor share and marginal costs.
- Numerical results show that this might work only on impact and for implausibly high values of ^F/_Y.

Theory: Search and Matching (SM) no capital

▶ return

- ► Wages as determined by nash bargaining, $w_t \neq \theta_t + lp_t$. [Galí, 2010]
- Hence s^h_t ≠ θ_t. The dynamics of the LS will differ since now wages and marginal product of labor behave differently.
- Considering only the extensive margin for now and again a linear production function y_t = n_t
- The labor share is now given by:

$$\boldsymbol{s}_t^h = \boldsymbol{w}_t \neq \theta_t$$

- Hence to generate an increase in the labor share the only possibility is to have a counter-factual response of wages to a monetary policy shock.
- Without wage rigidities, it would be difficult for wages to display a positive response given that the bargaining power of workers is bounded by one. The combination of both nominal wage and labor market rigidities, instead, proves to be enough to generate a positive response of real wages.



Parameter	Value/Uniform Prior Bounds	Description
β	0.990	Discount Factor
δ	0.025	Capital depreciation
Ē.	0.330	Steady State Hours
- Ŝ ^h	0.670	Steady State Labor Share
ς	$\frac{\lambda p}{\lambda p-1}$	elasticity of substitution between differentiated goods
FY	$\frac{1}{\zeta - 1}$	Fix costs over output
μ	$\frac{\lambda p}{\lambda p - 1}$	Elasticity of substitution between labour types
ŴС	$1 - \frac{1}{C}$	Steady State Marginal Costs
α	$1 - \bar{S}^h$	capital share
ϕ	[1,10.00]	Inverse of Frish Elasticity of Labor Supply
ϕ^{X}	[0.1,10]	Investment adjustment costs
ξp	[0,1]	Calvo price stickyness
ξw	[0,1]	Calvo wage stickyness
λ_D	[1.1,2]	price mark-up
λw	[1.1,2]	wage mark-up
ρ^r	[0,1]	Interest rate smoothing
θ^{π}	[1.01,5.00]	Taylor rule coeff of inflation
θУ	[0.0,1]	Taylor rule coeff of output
γ^{ρ}	[0,1]	Price Indexation
γ^{W}	[0,1]	Wage Indexation
ь	[0,1]	Habits in Consumption
ψ	[0,1]	Variable capital utilization

Table: Parameter Values

Table: Uniform prior distributions details - NK model

Parameter	Value/Uniform Prior Bounds	Description
β	0.990	Discount Factor
δ	0.025	Capital depreciation
Ĥ	0.330	Steady State Hours
- Ŝ ^h	0.670	Steady State Labor Share
ς	$\frac{\lambda p}{\lambda p - 1}$	elasticity of substitution between differentiated goods
μ	$\frac{\lambda p}{\lambda p - 1}$	Elasticity of substitution between labour types
ŴС	$1 - \frac{1}{c}$	Steady State Marginal Costs
F	$\frac{1}{\zeta-1}^{2}$	Fix costs over output
α	1 – <i>Š</i> ^h	capital share
σ_{c}	[1,10.00]	Intertemporal elasticity of substitution
_φ X	[0.1,10]	Investment adjustment costs
σ	[0.01,5]	Elasticity of Substitution between Capital and Labor
ξp	[0,1]	Calvo price stickyness
ξw	[0,1]	Calvo wage stickyness
λ_p	[1.1,2]	price mark-up
λ_W	[1.1,2]	wage mark-up
ρ'	[0,1]	Interest rate smoothing
θ^{π}	[1.01,5.00]	Taylor rule coeff of inflation
θ^{y}	[0,1]	Taylor rule coeff of output
γ^{ρ}	[0,1]	Price Indexation
γ^{W}	[0,1]	Wage Indexation
b	[0,1]	Habits in Consumption
ψ	[0,1]	Variable capital utilization

Table: Parameter Values

Table: Uniform prior distributions details - NK_CES model



Parameter	Value/Uniform Prior Bounds	Description
β	0.990	Discount Factor
δ	0.025	Capital depreciation
Ē	0.330	Steady State Hours
- Ŝ ^h	0.670	Steady State Labor Share
ς	$\frac{\lambda p}{\lambda p-1}$	elasticity of substitution between differentiated goods
F Y	$\frac{1}{\zeta-1}$	Fix costs over output
μ	$\frac{\lambda p}{\lambda p - 1}$	Elasticity of substitution between labour types
ŴС	$1 - \frac{1}{c}$	Steady State Marginal Costs
α	$1 - \bar{S}^h$	capital share
ϕ	[1,10.00]	Inverse of Frish Elasticity of Labor Supply
_φ X	[0.1,10]	Investment adjustment costs
ξp	[0,1]	Calvo price stickyness
ξw	[0,1]	Calvo wage stickyness
λ_p	[1.1,2]	price mark-up
λ_W	[1.1,2]	wage mark-up
ρ^r	[0,1]	Interest rate smoothing
θ^{π}	[1.01,5.00]	Taylor rule coeff of inflation
θŸ	[0.0,1]	Taylor rule coeff of output
γ^{p}	[0,1]	Price Indexation
γ^{W}	[0,1]	Wage Indexation
b	[0,1]	Habits in Consumption
ψ	[0,1]	Variable capital utilization
ν	[0,1]	working capital fraction

Table: Parameter Values

Table: Uniform prior distributions details - NK_WK model

Priors: NK_SM

Parameter	Value/Uniform Prior Bounds	Description
β	0.990	Discount Factor
δ^{k}	0.025	Capital depreciation
Ē	0.910	Steady State Employment
- Ŝ ^h	0.670	Steady State Labor Share
$\bar{\pi}$	2.25	inflation target
ς	$\frac{\lambda p}{\lambda p-1}$	elasticity of substitution between differentiated goods
F Y	$\frac{r_1}{\zeta - 1}$	Fix costs over output
σc	[1,10.00]	Intertemporal elasticity of substitution
b	[0,1]	Habits in Consumption
ϕ^{X}	[0.1,10]	Investment adjustment costs
ξ	[0,1]	Calvo price stickyness
λ_p	[1.1,2]	price mark-up
ν	[0,1]	working capital fraction
ψ	[0,1]	Variable capital utilization
θ	[0,1]	technology diffusion
ρ^{r}	[0,1]	Interest rate smoothing
θ^{π}	[1.01,5.00]	Taylor rule coeff of inflation
θY	[0.0,1]	Taylor rule coeff of output
δ	[0,1]	prob. of bargaining session determination
ŴŰ	[0,1]	Replacement Ratio
η^h	[0,2]	hiring fix cost relative to output %
η^{s}	[0,2]	search cost relative to output %
σ	[0,1]	matching function share of unemployment
ρ	[0,1]	job survival rate
Q	[0,1]	vacancy filling rate

Table: Uniform prior distributions details - NK_SM model





The wage stickiness Cumulative Density Function (CDF) on the left panels; in blue (red) the CDF that does (not) generate a positive response of the labor share. On the right panels, the combination of random draws from price and wage stickiness that do (not) verify the labor share IRF in blue (red). From top to bottom, the NK model, the NKCES model, and the NKCWRN model. **Bayesian IRF Matching**

- Let γ be the vector of parameter to estimate and Ψ(γ) denote the mapping from γ to the model IRFs.
- Let $\hat{\Psi}$ denote the corresponding empirical IRFs from the SVAR.
- $\hat{\Psi} \stackrel{a}{\sim} N(\Psi(\gamma^0), V(\gamma^0, \zeta^0, T)).$
- Approximate likelihood function

$$f(\hat{\Psi}|\gamma) = \left(\frac{1}{2\pi}\right)^{\frac{N}{2}} V^{-\frac{1}{2}} \exp\left[-\frac{1}{2}\left(\hat{\Psi} - \Psi(\gamma)\right)' V^{-1}\left(\hat{\Psi} - \Psi(\gamma)\right)\right].$$
(5)

- V is a diagonal matrix with the sample variances of the ψ's along the diagonal.
- So, given this choice of V, γ is effectively chosen so that Ψ(γ) lies as much as possible inside the Ψ̂'s confidence intervals.

return
Calibration

return

Description	NK	NK CES	NK WK	NK SM
Description		INC.OLO	MAL MAR	THE OWN
Discount Factor	0.99	0.99	0.99	0.99
Capital depreciation	0.025	0.025	0.025	0.025
Steady State Hours	0.330	0.330	0.330	-
Unemployment rate	-	-	-	5.5%
Steady State Labor Share	0.670	0.670	0.670	0.670
Inverse of Frish Elasticity of Labor Supply	1	-	1	1
Fix cost in production	calibrated to ensure 0 profits in steady state			
Relative Risk Aversion	1	1	1	1
wage mark-up	1.2	1.2	1.2	-
Elasticity of substitution between intermediate goods	$\frac{\lambda_p}{\lambda_p-1}$	$\frac{\lambda_p}{\lambda_p-1}$	$\frac{\lambda_p}{\lambda_p-1}$	$\frac{\lambda_p}{\lambda_p-1}$

For NK_SM model all the parameters not shown here are calibrated as in [Christiano et al., 2016]

Priors

return

Description	NK	NK_CES	NK_WK	NK_SM		
Investment adjustment costs	Γ(8, 2)					
Habits in Consumption	B(0.5, 0.15)					
Variable Capital Utilization	Γ(0.5, 0.3)					
Calvo price stickyness	B(0.66, 0.1)					
Calvo wage stickyness	B(0.66, 0.1)	B(0.66, 0.1)	B(0.66, 0.1)	-		
price mark-up (λ_n)	Γ(1.2, 0.05)					
Interest rate smoothing	B(0.7, 0.15)					
Taylor rule response to inflation		Г(1.7.	0.15)			
Taylor rule response to output	F(0.1, 0.05)					
Price Indexation	B(0.5, 0.15)	B(0.5, 0.15)	B(0.5, 0.15)	-		
Wage Indexation	B(0.5, 0.15)	B(0.5, 0.15)	B(0.5, 0.15)	-		
K/L elasticity of substitution	- /	N(1, 0.3)	-	-		
working capital fraction	-	-	B(0.8, 0.1)	B(0.8, 0.1)		
technology diffusion	-	-		B(0.5, 0.2)		
prob. of barg. session determination	-	-	-	Γ(0.5, 0.4)		
replacement ratio	-	-	-	B(0.4, 0.1)		
hiring fix cost relative to output %	-	-	-	Γ(1, 0.3)		
search cost relative to output %	-	-	-	Γ(0.1, 0.07)		
matching function share of unemployment	-	-	-	B(0.5, 0.1)		
job survival rate	-	-	-	B(0.8, 0.1)		
MP shock	Г(0.74, 0.05)					

Distributions: F Gamma, B Beta, N Normal.

Posterior Mode - US 11 VAR IRF Matching

return

Description	NK	NK_CES	NK_WKN	NK_SM
Investment adjustment costs	9.22 (5.78-12.84)	12.3 (6.56-18.9)	10.1 (6.55-13.8)	9.93 (6.39-13.6)
Habits in Consumption	0.78 (0.70-0.86)	0.88 (0.83-0.93)	0.81 (0.75- 0.87)	0.81 (0.74-0.87)
Variable Capital Utilization	0.63 (0.13-1.25)	0.93 (0.15-1.81)	0.73 (0.10-1.49)	0.18 (0.02-0.40)
Calvo price stickiness	0.79 (0.70-0.88)	0.78 (0.66-0.89)	0.66 (0.55-0.77)	0.60 (0.50-0.71)
Calvo wage stickiness	0.89 (0.85-0.94)	0.93 (0.90-0.96)	0.77 (0.66-0.86)	-
price markup	1.27 (1.18-1.37)	1.20 (1.10-1.30)	1.25 (1.17-1.34)	1.28 (0.19-1.37)
Interest rate smoothing	0.83 (0.80-0.87)	0.87 (0.84-0.91)	0.86 (0.83-0.89)	0.87 (0.83-0.90)
Taylor rule response to inflation	1.73 (1.45-2.02)	1.70 (1.41-2.00)	1.76 (1.49-2.03)	1.74 (1.47-2.03)
Taylor rule response to output	0.10 (0.01-0.19)	0.07 (0.01-0.14)	0.03 (0.01-0.05)	0.04 (0.01-0.07)
Price Indexation	0.63 (0.35-0.90)	0.59 (0.28-0.87)	-	-
Wage Indexation	0.47 (0.19-0.75)	0.51 (0.22-0.80)	-	-
K/L elasticity of substitution	-	0.67 (0.03-1.23)	-	-
working capital fraction (labor)	-	-	0.71 (0.40-1.00)	0.82 (0.66-0.97)
Intermediate inps share in prod.	-	-	0.58 (0.44-0.70)	-
working capital fraction (capital)	-	-	0.81 (0.53-1.00)	-
working capital fraction (intermediates)	-	-	0.82 (0.56-1.00)	-
technology diffusion	-	-	-	0.50 (0.12-0.87)
prob. of barg. session determination	-	-	-	0.50 (0.002-1.27)
replacement ratio	-	-	-	0.60 (0.39-0.80)
hiring fixed cost relative to output %	-	-	-	1.07 (0.52-1.67)
search cost relative to output %	-	-	-	0.05 (0.001-0.14)
matching function share of unemp.	-	-	-	0.46 (0.27-0.65)
job survival rate	-	-	-	0.33 (0.19-0.48)
MP shock stdev	0.77 (0.71-0.83)	0.76 (0.70-0.81)	0.75 (0.69-0.81)	0.75 (0.70-0.81)

Posterior mean of the parameters. 95% HDP interval in parenthesis.

IRF Matching - Matching only Federal Funds Rates and the Labor share



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